

Beyond Commodities and Industries: Accurate Measurement of Upstreamness in the Global Value Chain

Randall Jackson^a, Patricio Aroca^b, Erik Dietzenbacher^c and Umed Temursho^d

^aWest Virginia University Regional Research Institute, 886 Chestnut Ridge Rd, Morgantown WV, USA 26508; ^bCIUDHAD, Facultad de Economía y Negocios, Universidad Andrés Bello, Quillota 980, Viña del Mar, Chile.; ^cUniversity of Groningen, Netherlands ; and ^d IOpedia, Spain

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ABSTRACT

In two seminal papers, Antràs and Chor (2013, AC) and Antràs et al. (2012, ACFH) addressed the problem of measuring the degree to which industries are upstream or downstream in the global value chain. A growing number of publications have built upon their measurement formulation and accompanying computer code. Unfortunately, however, their implementation seems to be incorrect. The reason is that they work with data from supply–use tables (in a commodity-by-industry accounting framework) which are then processed as if the data were given by the interindustry flows from a standard input-output (IO) table. This paper takes the typical commodity-by-industry perspective into full account and derives two measures for upstreamness: a measure for the upstreamness of an industry and one for the upstreamness of a commodity. The difference between the standard Leontief-type IO table and the supply-use table developed by Stone is that the IO table assumes that each industry produces one and only one commodity. Stone’s framework recognizes that most industries produce more than one commodity, and most commodities are produced by more than one industry. This allows for taking secondary production into consideration. In this paper, we develop and implement properly formulated value chain metrics taking the Stone enhancements and their conceptual underpinnings into full account. We compare our results to the results from the incorrect formulations in AC and ACFH. We show that incorrect formulations have substantial empirical manifestations for some industries but not for other industries. We explain why this is the case.

KEYWORDS

Input-Output, SNA, Value Chains, Primary and Secondary Products

1. Introduction

In 1936, Wassily Leontief introduced the world to input-output accounting (Leontief, 1936). According to the press release announcing his selection as Nobel Prize awardee,

This important innovation has given to economic sciences an empirically-useful method to highlight the general interdependence in the production system of a society. In particular, the method provides tools for a systematic analysis of the complicated interindustry transactions in an economy. (Press Release: Nobel Media AB2020, 1973)

In building on Leontief’s foundations, Sir Richard Stone realized that secondary production by industries created consistency problems for national accounting and developed a critical refinement to the Leontief framework that treated industry use of commodities independently from commodity composition of industry output. A set of explicit accounting identities and algebraic manipulations support the construction of flows matrices that parallel the Leontief transactions matrices. This system of accounting eventually formed the basis for the United Nations Systems of National Accounts (United Nations, 1968).¹ In addition to supporting the construction of interindustry flow matrices, Stone’s framework further enabled representations of inter-commodity, commodity-by-industry, and industry-by-commodity accounts. “For having made fundamental contributions to the development of systems of national accounts and hence greatly improved the basis for empirical economic analysis,” Stone was awarded the 1984 Nobel Prize in Economics (Press Release: Nobel Media AB2020, 1984).

Despite these formal recognitions and widespread use in other disciplines and in public sector planning and investment decisions, and widespread acceptance and use internationally, neither the Leontief nor the Stone framework gained much traction in mainstream U.S. economics. Now, however, input-output models have attracted new attention in a variety of problem domains, such as life cycle accounting and inventorying, pollution emissions attribution, foreign content analysis, and value chains. Curiously, it is the Leontief inter-industry framework that often serves as the foundation for work by many – if not most – contemporary economists, despite the added power and versatility of Stone’s enhancements. Moreover, many of those engaged in empirical applications are failing to recognize or understand and appreciate the conceptual differences between the two frameworks and underlying data definitions and structures, and because nearly all nations now publish input-output data in the Stone framework, they are failing to match constructs to variables in the development and implementation of their new analytical metrics, even in top economics journals.

In this paper, we use an approach to the analysis of value chains that has gained substantial momentum as one among many possible examples that demonstrate the consequences of such conceptual misunderstandings, and by developing and implementing properly formulated value chain metrics, we demonstrate the ramifications of neglecting the Stone enhancements and their conceptual underpinnings. We discuss these issues in the context of value chain metrics, then take advantage of the Stone framework to develop conceptual and methodological consistency and demonstrate the consequences empirically by comparing the results from correct formulations to those from the incorrect formulations being replicated in the literature. We show that incorrect formulations can have substantial empirical manifestations.

Our primary objective is to draw researchers attention back to Stone’s developments

¹The UN SNA is not alone in adopting this framework. The OECD has adopted the Supply-Use framework (OECD, 2018), and the recently developed World Input-Output Database (Dietzenbacher et al., 2013) organizes it data similarly.

and call for the effort necessary to understanding properly the conceptual and theoretical foundations of modern systems of national accounts. Not only can the neglect of the differences in conceptual underpinnings of the two accounting systems lead to theoretical, conceptual, and empirical inconsistencies, but the additional information in the Stone supply-use framework can sometimes provide excellent avenues for problem solutions that are simply not available when analysis is limited only to Leontief accounts.

Our secondary objective is to highlight and support the critical role of modern publication policies that require that authors submit with their publications the code and data that enables reproduction of results. These resources can be extremely effective in supporting the knowledge building enterprise and the kinds of course corrections that ensure the integrity of and role for science in modern society. These policies are vitally important and scientists have a corresponding obligation to engage in reproducing published results and reporting issues encountered in the process.

The remainder of the paper is organized as follows. In the next section we introduce recent developments in value chain literature, and in so doing we begin to identify the confusion that can arise from a less than comprehensive understanding of the Stone framework and its underlying definitional and structural foundations. In section 3 we review the salient features of the Stone accounting framework, provide a corrected value chain measure that parallels the incorrectly implemented *upstreamness* measure in the literature, and demonstrate the consequences empirically. Section 4 returns to the basic definition of value chains and demonstrates one kind of analytical approach that can only be supported by the Stone framework, reinforcing the power, flexibility, and wider range of potential applications than can be developed and implemented in a Leontief framework. Section 5 discusses implications for practical application and for science and knowledge accumulation, and the final section summarizes the paper's contributions.

2. Value Chains

The characterization of global supply chains is a topic that has gained visibility and importance in recent literature. Various authors have approached supply and value chains from perspectives that include business transaction optimization, economic development policy, and property rights. An important case in point is a paper by Antràs and Chor (2013) (AC) that addressed the problem of measuring the degree to which industries are upstream or downstream in the global value chain, including an algorithm that they developed and used for these purposes. Since the 2013 AC publication and its companion, Antràs et al. (2012) (ACFH), a growing number of publications have built upon the incorrect measurement formulation and accompanying computer code. Unfortunately, their algorithmic implementation fails to recognize and account for the differences and distinctions between historical input-output (IO) accounting frameworks based on interindustry flows matrices on the one hand, and modern supply–use, or commodity-by-industry accounting frameworks on the other. Further, the realities of modern accounting frameworks make explicit the opportunity and need for researchers to identify differences in goals and objectives that might lead to the selection of alternative flows matrix formulations for identifying value chain *upstreamness* and *downstreamness*.

These two papers have introduced to the field an approach that overlooks the fundamental accounting relationships and identities of the current generation of IO account-

ing frameworks. In so doing, they have laid a potentially problematic foundation for a set of upstream and downstream production system linkage measures that is based on Leontief foundations but mis-applies data organized under the Stone accounting system. Whereas the availability of supporting code has facilitated the replication of the error by those who adopted it without scrutiny, it has also facilitated the critical assessment and corrective actions presented below.

2.1. Commodity Versus Industry: A Necessary Distinction

The statement “ $d_{ij}Y_j$, is precisely the value of commodity i used in j ’s production” (ACFH, page 414) refers to their formulation of the coefficient d_{ij} as an element of a Use table, and Y_j as industry j output. However, this definition is somewhat obscured by the fact that industries produce more than one commodity. Hence, d_{ij} would have a very different interpretation, and a different value, if it were drawn from a commodity-by-commodity IO table, in which the denominator would be the value of commodity rather than industry output. The choice of the denominator is critical to the interpretation and the value of d_{ij} , especially because the gross output of industry j can be very different from the gross output of commodity j . For example, the most upstream industry in their analysis based on 2002 U.S. data is the Petrochemical sector. Petrochemical *commodity* gross output is 22% larger than petrochemical *industry* gross output. This is because other industries also produce petrochemical commodities as a secondary product. The assumption that commodity and industry gross output are the same is quite clearly invalid.

The definitions of measures in AC are equally imprecise. For example, their “first measure is the ratio of the aggregate direct use to the aggregate total use (DUse_TUse) of a particular industry i ’s goods, where the direct_use for a pair of industries (i, j) is the value of goods from industry i directly used by firms in industry j to produce goods for final use, while the total use for (i, j) is the value of goods from industry i used either directly or indirectly (via purchases from upstream industries) in producing industry j ’s output for final use” (p. 2131). To be accurate and correct, the *direct use* definition would need to refer to an industry-by-industry intermediate transaction matrix, and the *total use* definition would need to refer to an industry-by-industry Leontief inverse matrix post-multiplied by a diagonal matrix of the total output by industry. Instead, they draw their data from a commodity-by-industry Use matrix to implement their measures. Neither reference to “the value of goods from industry i ” is accurate when the unadjusted Use matrix is the data source. The Use matrix is neither a flows matrix nor an industry-by-industry matrix.

To emphasize the importance of these distinctions, focus again on the Petrochemicals industry and commodity. Table 1 of Antràs et al. (2012), reproduced below as Table 1, identifies Petrochemicals (325110) as the industry with the highest upstreamness measure. However, the 2002 Make matrix companion to the Use table used for that analysis indicates that petrochemical commodities (products) account for only 36% of this industry’s total gross output. The remainder of the petrochemical indy’s gross output is secondary production, i.e., production of other commodities. Likewise, the petrochemicals industry produces only 44% of petrochemicals commodity output. The rest of the petrochemicals commodity production is secondary production from other industries.

Secondary production is precisely the reason why the commodity-by-industry framework for IO accounting was developed. Ignoring these definitional differences can result

Table 1. Least and Most Upstream Industries (Manuf.)

US IO2002 industry	Upstreamness
Automobile (336111)	1.000
Light truck and utility vehicle (336112)	1.001
Nonupholstered wood furniture (337112)	1.005
Upholstered household furniture (337121)	1.007
Footwear (316200)	1.007
Alumina refining (33131A)	3.814
Other basic organic chemical (325190)	3.853
Secondary smelting of aluminum (331314)	4.064
Primary smelting of copper (331411)	4.355
Petrochemical (325110)	4.651

Source: Authors' calculations, replicating Antràs et al. (2012, p. 415).

in substantial errors, mis-attributions, and misinterpretations. Therefore, we clarify and make explicit the relevant definitions and describe the ways in which the variables should be used in studying value chains. Analysts' choices of model structure will depend on whether the goal of the analysis is to identify commodities used to produce other commodities or in the industries involved in *interindustry* the production of commodities. If it is the former, then a commodity-by-commodity IO specification would be appropriate, while if it is the latter, one would presumably use an industry-by-commodity IO table. Likewise, an industry-by-industry model would be used when focusing explicitly on interactions among industries.² We review below the ACFH presentation so that we can assess whether the definition that is used in the paper relates to any of these alternatives, and if not, whether it is appropriate for their demonstration analysis.

2.2. The Upstreamness Measure

To develop their upstreamness measure, ACFH “begin by considering an N-industry closed economy with no inventories. For each industry $i \in 1, 2, \dots, N$, the value of gross output (Y_i) equals the sum of its use as a final good (F_i) and its use as an intermediate input to other industries (Z_i)” (p. 412).

$$Y_i = F_i + Z_i = F_i + \sum_{j=1}^N d_{ij} Y_j \quad (1)$$

They define d_{ij} as “the dollar amount of sector i 's output needed to produce one dollar's worth of industry j 's output.” This balance equation is correctly presented, provided that all variables are defined in industry space, i.e., Y , F , and Z are industry rather than commodity sectors, and that the term “sector i ” in the definition of d_{ij} refers to *industry* sector i .

They next derive equation (2), which is the Leontief inverse matrix expressed as an infinite series of terms that can be reduced to $Y = (I - D)^{-1}F$, where $(I - D)^{-1}$

²A post-processing option for some policy purposes might be to conduct the analysis in a commodity-by-commodity framework, and then convert to industry space using the standardized Make table to transform from commodity output to industry output, as described in Section 3, below.

is the traditional Leontief inverse. Based on these relationships and definitions, they then present their upstreamness measure, and describe it as “the (weighted) average position of an industry’s output in the value chain, by multiplying each of the terms in” (p. 413) the infinite series by their distance from final use plus one and dividing by the gross output of the industry. For industry i , this yields

$$U_{1i} = 1 \frac{F_i}{Y_i} + 2 \frac{\sum_{j=1}^N d_{ij} F_j}{Y_i} + 3 \frac{\sum_{j=1}^N \sum_{k=1}^N d_{ik} d_{kj} F_j}{Y_i} + 4 \frac{\sum_{j=1}^N \sum_{k=1}^N \sum_{l=1}^N d_{il} d_{lk} d_{kj} F_j}{Y_i} + \dots \quad (2)$$

Note that the denominator has changed now from Y_j to Y_i , a step that shifts the context from purchases to sales, and that they justify by noting that consideration should be taken of industries that sell to other upstream industries. They go on to provide a computational reduced form for this measure, after establishing its equivalence to Fally’s (2011) upstreamness measure, which has the following compact expression:

$$U_1 = (I - \Delta)^{-1} \cdot \mathbf{1} \quad (3)$$

“where Δ is the matrix with $\frac{d_{ij} Y_j}{Y_i}$ in entry (i, j) and $\mathbf{1}$ is a column vector of ones.” Finally, they “take the reciprocal to obtain *DownMeasure* for each industry i ” (Antràs and Chor, 2013, p. 2162). They go on to provide two economic interpretations for these upstreamness measures in which the emphasis appears to be linkages among industries and not products.^{3,4}

The conceptual inconsistency arises in the implementation of the upstreamness measure, which proceeds by replacing $d_{ij} Y_j$ in matrix Δ with U_{ij} , the ij^{th} cell from the Use matrix. Contrary to ACFH footnote 3, which states that “the coefficient d_{ij} is computed as the total purchases by industry j of *industry i ’s* output,” they draw coefficients from the Use table, which depicts the total purchases by industry j of *commodity i* , and not simply purchases from *industry i* . More than one industry can produce any given commodity, and the difference between industry and commodity output – as we have seen – can be substantial. More importantly, because commodities are produced by multiple industries, *the Use matrix is not a conventional flows matrix* as were the historical interindustry transactions matrices. While the columns of the Use matrix can be conceived of as destinations, the rows identify the commodities that each industry uses, but not the producing industries.

The inconsistency can be clarified further by returning to the derivation of the reduced form upstreamness expression from the power series expansion, which was derived from the accounting identity $Y_i = F_i + Z_i = F_i + \sum_{j=1}^N d_{ij} Y_j$. Consider the $d_{il} d_{lk} d_{kj}$ term of ACFH equation (2), where these d coefficients are defined as ratios of industry input dollar per industry output dollar. If we assign values of .1, .2, and .3 to these coefficients, then every dollar of output from industry j will require \$0.3

³We note that Dietzenbacher and Romero (2007) developed and reported measures that are virtually identical to these measures.

⁴The authors also make an open-economy adjustment, justified by noting that the data used to construct their matrix of US IO coefficients “do not distinguish between flows of domestic goods and international exchanges” (p. 414). The result is an adjustment factor for the IO coefficients matrix that transforms its interpretation from a technical relationship to a trade relationship. The adjustment factor is the ratio of domestic output of industry i to domestic use (absorption) of industry i output.

of input k , which will create a requirement for $\$(.2)(.3) = \0.06 of input l , which will then require $\$(.1)(.2)(.3) = \0.006 of input i for its production. The numerators and denominators have the same dimension (industry \$), so the interpretation of the product is clear and consistent. If, however, the d_{ij} coefficients have industry denominators but *commodity* numerators, then the product now reflects commodity i required to produce industry l output times commodity l required to produce industry k output times commodity k required to produce industry j output. But because each of these industries produces secondary products, the one-to-one relationship is lost; the product of this multiplication can only make sense dimensionally, and can therefore only have an unambiguously straightforward interpretation *if and only if* these industries produce only their own commodities, which would mean that industry and commodity output would have to be identical. This kind of system would be reflected in a Make table with nonzero elements only on the diagonal. Were these coefficients defined with commodity terms in both numerator and denominator, they would be interpreted as commodity i required in the production of commodity l times commodity l required in the production of commodity k times commodity k required to produce commodity j , and this would be dimensionally consistent.

The crux of the problem is that commodity required to satisfy industry demand results not only in the production of the industry's primary commodity, but also the production of secondary commodities, and this happens at every term in the power series expansion, resulting in the loss of ability to trace commodities unambiguously through the supply chain.

3. The Stone Framework and Upstreamness Reformulation

The values in the Use table are associated behaviorally with columns. They represent column industry requirements of row commodity inputs, so standardizing by row commodity output values is not particularly useful. This does not render the development of an ACFH-type upstreamness measure intractable, of course. The modern accounting system that is the commodity-by-industry framework was devised precisely to accommodate the need to work analytically with systems in which industries produce multiple commodities. Indeed, developing the linkage matrices in industry-by-industry, commodity-by-commodity, industry-by commodity, and even commodity-by-industry format is possible using precisely the same database that ACFH used to implement their measure. We provide below the fundamental accounting equations that support the construction of these requirements coefficients tables.

3.1. Conceptual Reformulation

The commodity-by-industry framework is presented below in Figure 1. In conventional IO notation (as in Miller and Blair, 1985, 2009), the matrix partition $U = [u_{ij}]$ is the Use matrix, $V = [v_{ij}]$ is the Make matrix, e is commodity final demand expressed here as a single vector, q is commodity gross output, and g is industry gross output. Only in highly unusual cases will an industry produce no secondary commodities, so rarely will q_i and g_i be equal. The *va* term denotes value added.

The traditional industry output balance equation that ACFH write as $Y_i = F_i + Z_i$ actually has no simple and direct counterpart in the modern accounting framework (although one can be derived, it requires assumptions about secondary production

technology and information contained in V).⁵ We can, however, express a commodity output balance equation in this conventional notation as $q_i = \sum_{j=1}^N u_{ij} + e_i$, and we can further define $d_{ij} = \frac{u_{ij}}{g_j}$ and substitute to obtain $q_i = \sum_{j=1}^N d_{ij}g_j + e_i$, maintaining the output balance.

Figure 1. The Commodity-Industry Framework

	Commodities	Industries	Final Demand	Totals
Commodities		U	e	q
Industries	V			g
Primary Inputs		va		
Totals	q'	g'		

In matrix notation, we have the following identities:

$$U\mathbf{i} + e \equiv q \quad (4a)$$

$$V\mathbf{i} \equiv g \quad (4b)$$

$$V'\mathbf{i} \equiv q \quad (4c)$$

where \mathbf{i} is a summing vector, and $'$ signifies the transpose operation. We define behavioral relationships as follows:

$$B = U\hat{g}^{-1} \quad (5a)$$

$$U = B\hat{g} \quad (5b)$$

$$D = V\hat{q}^{-1} \quad (5c)$$

$$V = D\hat{q} \quad (5d)$$

where $\hat{\cdot}$ indicates diagonalization. Equation 5a defines the production requirements of commodities per industry output dollar, and equation 5b is a statement of the industry-based technology assumption that commodities are produced by industries in fixed proportions.⁶ Note that the effect of pre-multiplication of a commodity vector or matrix by D results in a transformation from commodity-space to industry-space, so $V\mathbf{i} = g = Dq$. This system allows us to formulate the following commodity balance equation:

$$q = Bg + e \quad (6a)$$

$$q = BDq + e \quad (6b)$$

$$q = (I - BD)^{-1}e \quad (6c)$$

The BD term is a commodity-by-commodity requirements matrix counterpart to the classical, column-standardized interindustry Leontief IO coefficients matrix. Equation 13 is the reduced form solution for q as a function of commodity final demand, e .

⁵The industry output balance equation is conventionally denoted $X=Y+Z$.

⁶The alternative is the commodity-based technology assumption, which while not used here, could be developed in parallel fashion.

This expression, however, is consistent with the Leontief demand driven formulation, in which the values in the Use matrix are divided by their respective column industry output values. In contrast, the upstreamness measure in AC (and ACFH) shown in equation 3 is formed by dividing the elements in the Use matrix by respective *row commodity* output, although they refer to this as row *industry* output.⁷ To convert the BD matrix to an equivalent and correctly formulated (Ghoshian) matrix, we can return the BD coefficients to their transactions values using UD , then standardize the rows by commodity output, q , yielding $\hat{q}^{-1}UD$. The difference between the incorrect $\hat{q}^{-1}U$ formulation and the correct reformulation is quite clearly the D term, which is the essential mechanism that transforms the industry column dimension of the Use matrix to the commodity output space of vector q . The other difference is that ACFH convert commodity output to commodity absorption by netting out trade and inventories, which can be implemented similarly in the new commodity-by-commodity requirements matrix reformulation by adjusting q for net trade and inventory adjustment before using it as a standardizing vector.⁸

3.2. Empirical Example

With the conceptual distinction established, we turn in this section to a demonstration of the empirical consequences for the computed measures reported in ACFH. Table 2 displays upstreamness scores replicated using the ACFH algorithm and data and using the corrected algorithm presented in this paper and the ACFH data. The top seven rows of data report results for the commodity sectors whose scores rank among the top five using either method, and the last six rows correspond to the five lowest ranking commodity sectors using either method. Each row shows the scores for sectors that rank highest in the first data column, their ACFH ranks in the second data column, their scores from the reformulated algorithm in the third data column, and their respective ranks in the fourth.

Note first that there is a good deal of commonality. The ranks in the lowest ranking sectors are quite similar, which would be expected a) because both formulations rank commodities and not industries, b) because of the general correspondence between industries and commodities, especially for industries producing consumer products, although even here, Footwear Manufacturing shows an 8-point difference in ranks, and c) because sectors with the lowest scores are virtually never used as intermediate inputs and are therefore much less distinguishable in their upstreamness scores. There is somewhat greater discrepancy in the highest ranked sectors, however, where rank differences are as great as 16 among only the five most highly ranked upstreamness sectors. Indeed, the average difference in ranks is 7, due to the notable ranking shifts for Other Basic Organic Chemical Manufacturing, Steel Product Manufacturing from Purchased Steel, and Primary Smelting and Refining of Nonferrous Metals (except copper and aluminum).

The reformulation reveals substantial differences. Because of the multi-commodity reality of industry production, the second and fifth highest ranking upstreamness sec-

⁷We confirm the authors' stated intent via reference to the publications, but we confirmed their implementations by evaluating the code that accompanies those publications.

⁸The $B\hat{D}$ matrix, where \hat{D} is the Make matrix standardized by q adjusted for net trade and inventory, would be used in the computation of the counterpart, commodity-by-commodity downstreamness measure used in Antràs and Chor (2013). Although we have not addressed explicitly the derivation and use of the counterpart interindustry rather than inter-commodity measures, the development would follow a similar path but would be based on row- or column-standardization of the interindustry transactions matrix $\hat{D}U$. This formulation based on the modification of the D matrix is introduced in Jackson (1998).

Table 2. Upstreamness measure comparisons

NAICS	Sector	ACFH		Corrected CxC	
		Score	Rank	Score	Rank
325110	Petrochemical mfg	4.6511	1	4.1785	4
331411	Primary copper smelting and refining	4.3547	2	6.4031	1
331314	Secondary aluminum smelt & alloying	4.0637	3	3.9991	6
325190	<i>Other basic organic chemical mfg</i>	3.8529	4	3.5391	15
33131A	Alum. primary prodn and refining	3.8144	5	4.9632	3
331200	<i>Steel product from purchased steel</i>	3.45	16	4.0065	5
331419	<i>Prim. nonfer. metal smelt & refn</i>	3.4186	18	5.6283	2
336111	Automobile mfg	1.0003	279	1.0004	279
336112	Light truck and utility vehicle mfg	1.0005	278	1.0008	278
337122	Wood HH furniture mfg.	1.0052	277	1.0072	277
337121	Upholstered HH furniture mfg	1.0072	276	1.008	276
316200	<i>Footwear mfg</i>	1.0073	275	1.0454	267
336213	Motor home mfg	1.0123	274	1.0129	275

Source: Antràs et al. (2012) and authors' calculations. Largest ranking differences in bold.

tors using the correct method are not even in the top 15 sectors using the earlier formulation. Secondary production strongly influences the upstreamness measures, and cannot be ignored in implementation.

To demonstrate the inaccuracies introduced in counterpart downstreamness measures, we replicate AC's results for their DownMeasure (AC, page 2163) and provide in Table 3 corrected rankings for their highlighted industries. In Table 4 we provide the correctly ranked and highlighted industries that we obtain when using the correctly formulated commodity-by-commodity matrices along with the AC rankings. As with the upstreamness comparisons, there is some substantial agreement, but there also are some very substantial differences.

Table 3. DownMeasure Comparisons: AC Results

	Industry	<u>AC</u>		<u>Corrected CxC</u>
		DownMeasure	Rank	Rank
Lowest 10 Values				
325110	Petrochemical mfg	0.2150	253	250
331411	Primary copper smelt & refining	0.2296	252	253
331314	Secondary aluminum smelt & alloy	0.2461	251	247
325190	Other basic organic chemical mfg	0.2595	250	241
33131A	Primary alumina refin and prodn	0.2622	249	251
325310	Fertilizer mfg	0.2658	248	248
335991	Carbon and graphite product mfg	0.2668	247	246
325181	<i>Alkalies and chlorine mfg</i>	0.2769	246	224
331420	Copper rolling, drawing, etc.	0.2769	245	244
325211	<i>Plastics material and resin mfg</i>	0.2800	244	219
Highest 10 values				
339930	<i>Doll, toy, and game mfg</i>	0.9705	10	20
311111	Dog and cat food mfg	0.9717	9	7
337910	Mattress mfg	0.9720	8	8
315230	<i>Women's and girls' apparel mfg</i>	0.9762	7	17
321991	Manufactured home mfg	0.9810	6	6
336212	Truck trailer mfg	0.9837	5	5
336213	Motor home mfg	0.9879	4	4
316200	Footwear mfg	0.9927	3	3
337121	Upholstered HH furniture mfg.	0.9928	2	2
336111	Automobile mfg	0.9997	1	1

Source: Antràs and Chor (2013) from authors' calculations. Largest rank differences in bold.

Table 4. DownMeasure Comparisons: Corrected CxC Results

	Industry	<u>Corrected CxC</u>		<u>AC</u>
		DownMeasure	Rank	Rank
Lowest 10 Values				
331411	Primary copper smelt & refining	0.1597	253	252
331419	<i>Primary nonferrous smelt & refin</i>	0.1804	252	236
33131A	Primary alumina refin and prodn	0.2049	251	249
325110	Petrochemical mfg	0.2467	250	253
331200	<i>Steel product mfg from purch steel</i>	0.2560	249	238
325310	Fertilizer manufacturing	0.2698	248	248
331314	Secondary aluminum smelt & alloy	0.2703	247	251
335991	Carbon and graphite product mfg	0.2735	246	247
333612	<i>Industrial drive and gear mfg</i>	0.2743	245	205
331420	Copper rolling, drawing, etc.	0.2750	244	245
Highest 10 values				
311230	<i>Breakfast cereal manufacturing</i>	0.9629	10	15
336612	Boat building	0.9700	9	11
337910	Mattress manufacturing	0.9725	8	8
311111	Dog and cat food manufacturing	0.9786	7	9
321991	Manufactured home mfg	0.9818	6	6
336212	Truck trailer manufacturing	0.9855	5	5
336213	Motor home manufacturing	0.9874	4	4
316200	Footwear manufacturing	0.9917	3	3
337121	Upholstered household furniture mfg	0.9931	2	2
336111	Automobile manufacturing	0.9996	1	1

Source: Antràs and Chor (2013) and authors' calculations. Largest rank differences in bold.

4. Consistency with the Value Chain Construct

Although we have provided a correct commodity-by-commodity upstreamness measure, the appropriateness of interpretation remains unaddressed. According to Kaplinsky and Morris (2001), a simple value chain “describes the full range of activities which are required to bring a product or service from conception, through the different phases of production (involving a combination of physical transformation and the input of various producer services), delivery to final consumers, and final disposal after use.” In our Stone accounting framework, industries are the activities and commodities are the products. Therefore, a formulation that more precisely captures the spirit of the value chain definition would be an industry-by-commodity framework rather than a commodity by commodity framework, because rather than simply identifying the commodity production required to bring a commodity to market, the industry-by-commodity framework quantifies the range of activities by industry.⁹ Further, adding other dimensions of the “range of activities,” such as employment and income, or ancillary variables like water use or emissions, requires that the activity levels be quantified by industry and not by commodity. For these reasons, the industry-by-commodity formulation is preferred when quantifying activity levels. Simply knowing what commodities are required in a value chain falls short of identifying required activity.

The power of the Stone framework as an analytical tool is demonstrated here yet again, as the transformation of a Ghoshian- or Leontief-type framework from commodity-by-commodity to industry-by-commodity space is straightforward and can be achieved simply by pre-multiplying the respective inverse matrices by D , or

$$D(I - \hat{q}^{-1}UD)^{-1} \tag{7}$$

for the Ghoshian-type formulation and

$$D(I - BD)^{-1} \tag{8}$$

for a Leontief-type inverse transformation.

In Table 5, we replicate Table 3, substituting the new and properly formulated industry rankings derived from the industry-by-commodity Ghoshian formulation of equation 7 for the *Corrected IxC* results column. As before, while there are some similarities, the difference now are stark. Of the sectors with the ten smallest values in AC’s ranking (those with the highest upstreamness), only five are in the comparably defined new set. Further, the average absolute difference in ranks between the AC and new top ten (upstream) sectors is now 27.3. AC’s *most* upstream sector becomes the just 71st most upstream sector ($253 - 183 + 1 = 71$), and their 8th most upstream sector is the 108th in the new rankings.

Table 6 replicates Table 4, where the top ten sectors ranked highest and lowest using the correct industry-by-commodity formulation are shown, along with their corresponding AC rankings. Again, we see major discrepancies, including the new second lowest ranking – second most upstream – sector now corresponding to the 96th most upstream sector in the AC ranking, and an average absolute difference in ranks for the most upstream sectors of 30.3. Commodity-by-commodity rankings clearly misidentify

⁹Of course, no input-output formulations capture the entire value chain through distribution and post-use disposal.

Table 5. DownMeasure Comparisons: AC and I-by-C Results

		AC		Corrected IxC
	Industry	DownMeasure	Rank	Rank
Code	Smallest 10 Values			
325110	Petrochemical manufacturing	0,2150	253	183
331411	Primary copper smelt \& refining	0,2296	252	225
331314	Secondary aluminum smelt	0,2461	251	204
325190	Other basic organic chemical mfg	0,2595	250	253
33131A	Primary aluminum refining \&prod	0,2622	249	250
325310	Fertilizer manufacturing	0,2658	248	237
335991	Carbon and graphite product mfg	0,2668	247	244
325181	Alkalies and chlorine mfg	0,2769	246	146
331420	Copper rolling, drawing, extruding	0,2769	245	249
325211	Plastics material and resin mfg	0,2800	244	251
Code	Highest 10 Values			
339930	Doll, toy, and game manufacturing	0,9705	10	2
311111	Dog and cat food manufacturing	0,9717	9	38
337910	Mattress manufacturing	0,9720	8	37
315230	Women's cut and sew apparel	0,9762	7	5
321991	Manufactured home mfg	0,9810	6	29
336212	Truck trailer manufacturing	0,9837	5	26
336213	Motor home manufacturing	0,9879	4	48
316200	Footwear manufacturing	0,9927	3	1
337121	Upholstered hh furniture mfg	0,9928	2	24
336111	Automobile manufacturing	0,9997	1	9

Source: Antràs and Chor (2013) from authors' calculations. Largest rank differences in bold.

Table 6. DownMeasure Comparisons: AC with IxC Results

		Corrected IxC		AC
	Industry	DownMeasure	Rank	Rank
Code	Smallest 10 Values			
325190	Other basic organic chemical mfg	0,1921	253	250
324110	Petroleum refineries	0,1944	252	158
325211	Plastics material and resin mfg	0,2246	251	244
33131A	Alumina refining and primary prod	0,2329	250	249
331420	Copper rolling, drawing, extruding	0,2330	249	245
331490	Nonferrous metal rolling, drawing	0,2592	248	235
322120	Paper mills	0,2617	247	192
323110	Printing	0,2628	246	174
332600	Spring and wire product mfg	0,2657	245	194
335991	Carbon and graphite product mfg	0,2786	244	247
Code	Highest 10 values			
316900	Other leather and allied product mfg	1,5720	10	88
336111	Automobile manufacturing	1,5849	9	1
315900	Apparel accessories mfg	1,7072	8	51
333315	Photo and copying equipment mfg	1,7746	7	28
339910	Jewelry and silverware mfg	1,9089	6	34
315230	Women's cut and sew apparel mfg	1,9662	5	7
315220	Men's cut and sew apparel mfg	2,3624	4	20
315290	Other cut and sew apparel mfg	3,1213	3	30
339930	Doll, toy, and game mfg	3,2026	2	10
316200	Footwear manufacturing	9,1246	1	3

Source: Antràs and Chor (2013) from authors' calculations. Largest rank differences in bold.

the industry activity rankings, and any policy or programmatic actions based on the incorrect rankings will be poorly targeted.

5. Discussion

There are two primary contributions of the work reported here. First, there are the implications for those whose practical applications will be founded on the now-dominant Stone-type IO frameworks instead of the classical Leontief interindustry accounts. The second contribution lies in the demonstration of the value to science of modern publication policies that support reproducible research. In this section, we elaborate on both areas.

5.1. Implications for Practical Application

The need for the correction in formulation arises from the existence of secondary commodity production by industries. Hence, for an economy whose Make table is strongly diagonal – one with very little secondary production, empirical results might well differ little as a result of our correction, but the differences will become more substantial as the ratio of off-diagonal supply-table elements to diagonal elements increases. The degree of difference for a given set of accounts is an open empirical question, in that primary and secondary production structures vary geographically.

Because these metrics will most often be used in practice to identify and prioritize industries for further or attention, higher ranked industries will be of most interest and greatest value to anyone carrying out this kind of analysis. Therefore, the rank order correlations over the entire vector of ranks are not as relevant to the analyst as is the ability to correctly identify the top ranked industries. Below we present two additional perspectives on the impacts of the correct formulation that underscore its importance in practical application.

First, we compute and display graphically the differences in ranks over the entire distribution of industries for which the measure has been calculated. Although correlations between the entire corrected and uncorrected upstreamness or downstreamness vectors can be quite strong, the differences in individual ranks can be quite substantial. Figure 2 presents a plot of the simple differences in ranks for vectors of correct industry-by-commodity and uncorrected commodity-by-commodity values for the upstreamness measure derived from the same 2002 U.S. data used in ACFH, with sectors ordered according to their original industry classification scheme sequence.

Next, we set up the following analysis, again using the same data. We first rank order sectors using the corrected measure values. We assign a value of 1 for $n = 1$ (where rank order calculations cannot be computed), then, we sequentially increase n by 1. As n increases, we select the top n corrected-ranked sectors from the incorrect vector, generate ranks for values within that set of n sectors, and then compute the Spearman rank correlations between vectors of sequentially increasing lengths. The result is a set of rank correlations for sets of vectors of incrementally larger dimension. The correlations are actually best-case comparisons, because in most sets, uncorrected sector rank values from the entire set of industries will most often exceed the value of n , but for the correlations to be valid, their ranks are indexed relative to the n values in each vector in the comparison set. The result of that exercise for $n = 1, \dots, 40$ is shown below in Figure 3, which reveals that at $n = 5$, there is 0.2 correlation; for the top 10 ranked correctly calculated values, the correlation rises to 0.6, and by $n = 40$,

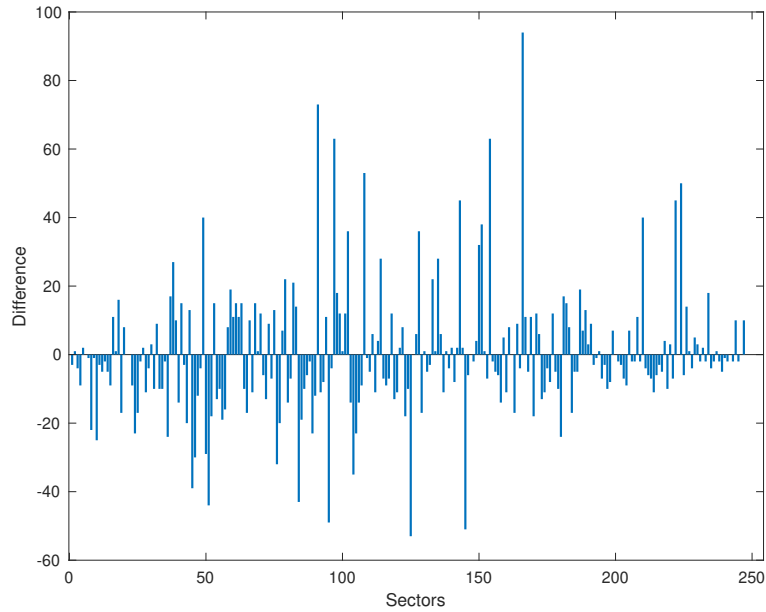


Figure 2. Downstreamness: Difference in Ranks

the correlation is still only 0.65. While there is no clear way of assessing the statistical significance of these sequential comparisons, the two ranks-vectors are clearly not correlated strongly enough to suggest that there is only insubstantial difference in the qualitative nature of the results, and certainly no support for simply ignoring the effect that the correction has on outcomes.

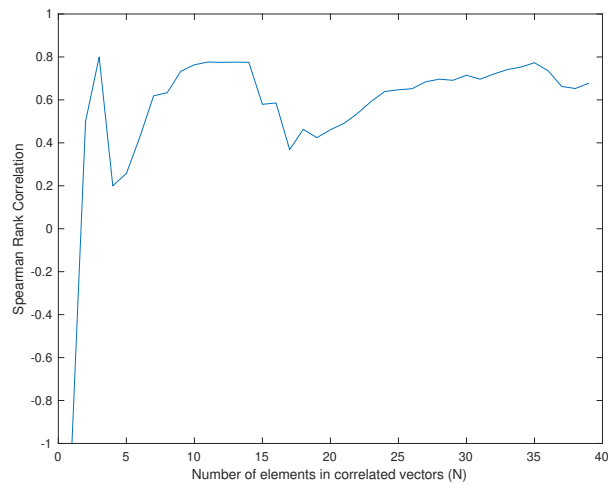


Figure 3. Downstreamness: Spearman Rank Comparison for Top n Ranks

Irrespective of the empirical implications, of course, a published use table in isolation provides only a partial description of an IO system. This alone is reason enough to base empirical analyses on the correct formulations. The correction is straightforward and the necessary Make table data are virtually always published in tandem, so there is no reason not to use the correct formulation.

Yet the incorrect formulation continues to be used and are becoming increasingly entrenched in the literature, as noted in Section 2.

5.2. *Implications for Science and Knowledge Accumulation*

“Replication is the cornerstone of science. Research that cannot be replicated is not science, and cannot be trusted either as part of the profession’s accumulated body of knowledge or as a basis for policy. Authors may think they have written perfect code for their bug-free software package and correctly transcribed each data point, but readers cannot safely assume that these error-prone activities have been executed flawlessly until the authors’ efforts have been independently verified.” (McCullough and Vinod, 2003, p. 888)

In 2004, the *American Economic Review* joined a growing number of other academic journals and “began requiring ‘data and code sufficient to permit replication’ of a paper’s results, which is then posted on the journal’s website.”¹⁰ This paper aligns with the spirit of these publication policies¹¹ by providing an important course correction for those who might otherwise continue to use errant code submitted with published contributions. We have presented the correct formulations and new code for the corrected algorithm, and we have identified data consistent with the new algorithmic formulation. Our corrections also identify important conceptual considerations that future analysts will overlook at peril of arriving at faulty and misleading conclusions at best, and ill-formulated policy and programmatic recommendations at worst.

Had the original two papers merely faded in importance and use, such corrections would be less critical. On the contrary, however, as of late September of 2020, these two papers had been cited more than 260 times, with more than half (120) of these citations in the most recent 20 months, many in top economics journals.¹² Those directly citing articles, in turn, had been cited more than 2,500 times, according to the Web of Science Citation Index. Further, although we have not checked each and every citing article, we have not identified a single one that rectifies the issues we have identified, and every application that we have been able to assess appears to use precisely the same errant code provided by the authors. Without an explicit correction, these and related errors will continue to propagate.

Conconi et al. (2018) and Alfaro et al. (2019), for example, reused the errant Antras code in their application, and further replaced row and column sector names with corresponding harmonized sector product names. This not only created the false appearance of a product-by-product transactions matrix, but this naming replacement step also deepened conceptual confusion because it resulted in some ‘duplicate’ sectors, which then they dealt with by inexplicably replacing several product columns in coefficient tables with the averages of their corresponding coefficient values.¹³ Had the necessary attention been paid to the precise definitions and structure of the underlying supporting data upon first publication, such compounding errors could have been avoided.

¹⁰https://en.wikipedia.org/wiki/The_American_Economic_Review#cite_note-5 Accessed 9/2/2020.

¹¹“Authors of accepted papers that contain empirical work, simulations, or experimental work must provide, prior to acceptance, information about the data, programs, and other details of the computations sufficient to permit replication, as well as information about access to data and programs.” <https://www.aeaweb.org/journals/policies/data-code/> Accessed 9/2/2020

¹²A sample of direct citations from 2020 alone includes Antràs and de Gortari (2020); Choi (2020); Kostoska et al. (2020); Li et al. (2020); Murakami and Otsuka (2020); Peng and Zhang (2020); Shen and Zheng (2020).

¹³At best, averaging two or more coefficients columns implies that the transactions values all have equal weights, despite the fact that the values initially used in standardize the columns are clearly unequal.

There is also increasing evidence throughout the economics literature that industries and products are being treated as though they were equivalent. Kee and Tang (2016), for example, have adopted this practice in research on geographical sources of value added in Chinese exports, in which they note that “Industries are defined according to the industry classification by the United Nations,” and footnote details on which products from the Harmonized Commodity Description and Coding Systems (HS) were their foci. But by assigning products to individual producing industries, they are implicitly assuming a kind of sectoral equivalence that simply does not exist. If industry-specific implications are important for such studies, then introduced bias might be quite substantial and potentially important. In this and some related contexts, there might not be particularly good ready alternatives, but the bias that is introduced via such implicit assumptions should be made explicit.

The power of IO frameworks is being newly and appropriately recognized in a growing number of problem domains, but equally important to the development of conceptualizations and analytical tools in new application areas is the need to understand how and even why the supporting data were generated. Matching variables to constructs is as important to IO analysts as understanding data generating processes is to econometricians. Industries and commodities are not conceptual equivalents; organization frameworks like those of Leontief and Stone have different conceptual underpinnings; and data and classification systems themselves are designed for specific purposes, as data providing agencies strive to make clear. The U.S. Census website, for example, notes explicitly that, “NAICS is an industry classification system, not a product classification system, and therefore neither intended nor well suited for this purpose.” (US Census Bureau, 2020)

The examples in this section underscore the value of publication policies that emphasize transparency and replication. At a time when science is increasingly under attack, supplying readers with the tools needed for replication is vitally important, as is carrying out such research replications and reporting on those that reveal conceptual or empirical deficiencies. Those with expertise in data generation can join algorithmic and problem domain experts to ensure the integrity of the scientific enterprise. Further, when code accompanying publications is found to be in error, journals in which it is published must curtail its propagation without delay by removing and, when possible, replacing it with corrected code or a reference to appropriate sources. If we fail to engage in replication, if we fail to acknowledge research shortcomings, and if we fail to communicate necessary course corrections, then we relinquish all rights to the defense of science and fall sadly short of our responsibilities as scientists.

6. Summary

In this paper, we identified an important inconsistency in the formulation and implementation of upstreamness and downstreamness measures developed and presented in AC and ACFH. The lack of correspondence between construct and data has carried through to numerous subsequent publications identified in the introduction, necessarily generating inaccurate results. The problem arises because important differences between historical interindustry and modern commodity-by-industry IO accounting frameworks are overlooked. We develop and implement a correctly formulated and conceptually consistent alternative based on the commodity-by-industry framework that meets the objectives of the upstreamness and downstreamness measures. Our empirical demonstration makes clear the need to use the correct formulation when

studying production linkages.

The options available to those studying upstream and downstream linkages in the context of supply and value chains are also worth considering, because each of these options produces a different kind of information. First, one can formulate these measures to study either commodity or industry chains. Commodity chain analyses will reveal information about the production of selected products, while industry supply chains can reveal information about the linkages among activities, specifically industries that are engaged in the production of one or more products. Industry and commodity linkages are surely different, and depending on the goal of the analysis, one or the other classification may be preferred. Second, the coefficients that define the interactions among commodities or industries can be purged of trade as in the procedures discussed here, and this provides a focus on the within-region (in this case, nation) production chains. However, the coefficients also can be based on technical requirements irrespective of origin, and this can provide information that can be useful in assessing the production structure of an economy relative to potential development alternatives.

Contrary to complicating the accounting framework, the format of modern systems of national accounts actually enriches the possibilities for meaningful analysis, and facilitates analyses of products (commodities) and activities (industries) in economic systems. Time and effort spent deepening awareness and understanding of the underlying accounting conventions and embedded relationships can yield substantial research and application dividends.

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